

## Alg2T Warm Up Ch 4 Day 4

\*\*\*Quiz Friday 21st

If the solution to the equation  $(x+a)(x+b) = 0$  are  $x = 6$  and  $x = -4$ , then  $a + b = ?$ 

- F. -24
- G. -12
- H. -2
- J. 2
- K. 24

Monday 24th

Which of the following are the values of  $x$  for which  $2x^2 = 3 - 5x$ ?

- A.  $-\frac{1}{2}$  and 3
- B. -1 and  $\frac{3}{2}$
- C.  $-\frac{3}{2}$  and 1
- D. -2 and 3
- E. -3 and  $\frac{1}{2}$

## Homework Questions???????

Let's look at #62

$h = -16t^2 + 32t + 6$ , find the maximum height of the baton.

20.)  $169/4, (x-13/2)^2$

22.)  $-2 \pm \sqrt{14}$

24.)  $-3 \pm 2\sqrt{3}$

28.)  $-4 \pm \sqrt{10}$

30.)  $5 \pm 2\sqrt{7}$

42.)  $y = (x-2)^2 - 5, (2, -5)$

44.)  $y = (x+10)^2 - 10, (-10, -10)$

50.)  $x = -5 \pm 2\sqrt{3}$

62.) 22ft

## Worksheet 4.7

#'s 10-14, 17, 20, 22, 26, 27

## Warm Up

What value of  $c$  makes the trinomial a perfect square binomial. Write the trinomial as a square binomial.

1.)  $x^2 + 10x + c$

Solve by completing the square.

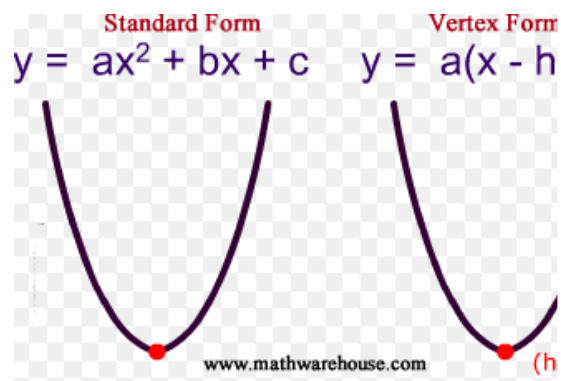
2.)  $x^2 - 14x + 9 = 0$

II. Use completing the square to solve. TOYO:

4.)  $3x^2 + 12x - 18 = 0$

Example  
III. Write in vertex form. Identify the vertex.

1.)  $y = x^2 + 2x + 5$



Write in vertex form. Identify the vertex.

$$y = x^2 - 4x + 10$$

Algebra 2 Trig Daily Learning Target Quiz  
Completing the Square Day 4

|   |  |
|---|--|
| <p>1.) Find the <math>c</math> value that makes the expression a perfect trinomial. Then rewrite as a binomial squared.</p> $x^2 - 14x + c$ | <p>2.) Solve.</p> $x^2 + 8x + 4 = 0$           |
| <p>3.) Write in vertex form.</p> $y = x^2 - 6x + 5$   | <p>4.) What does it mean to be a solution?</p> |



## Alg2T Extra Credit Ch 4 Day 4

For which of the following values of  $b$  will there be 2 distinct real solutions to the equation  $2x^2 - bx + 6 = 0$  ?

- F.  $4\sqrt{3}$
- G.  $-4\sqrt{3}$
- H.  $-2$
- J.  $0$
- K.  $7$

**Ch 4**  
**Quadratic Functions**  
**(4.8/4.6)Quadratic**  
**Formula, The**  
**Discriminant, and**  
**Imaginary**

## The Quadratic Formula

We can sing, if  
you want to...

[https://  
www.youtube.com/  
watch?  
v=2lbABbfU6Zc](https://www.youtube.com/watch?v=2lbABbfU6Zc)

*If  $y = ax^2 + bx + c$*

*then the  $x$  – intercepts or roots are*

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

I. Use the quadratic formula to solve.

Example

1.)  $3x^2 + 8x = 35$

I. Use the quadratic formula to solve.

Example

2.)  $12x - 5 = 2x^2 + 13$

I. Use the quadratic formula to solve.

Example

3.)  $-2x^2 = -2x + 3$

## The Discriminant

$$b^2 - 4ac$$

What is it good for?

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad \leftarrow \text{the } b^2 - 4ac \text{ part is the Discriminant}$$

When:

$$b^2 - 4ac = 0$$

↓

1 double root

Note: "root" - means solutions

$$b^2 - 4ac = \text{positive}$$

↓

2 real roots

$$b^2 - 4ac = \text{negative}$$

↓

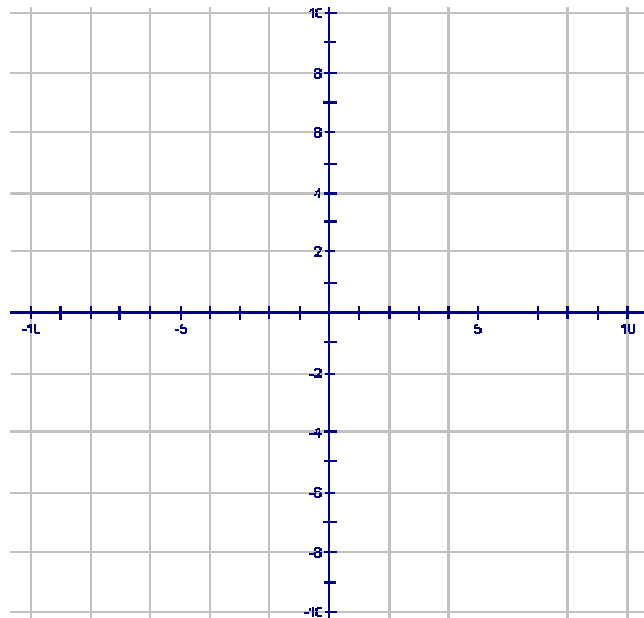
No real roots

or  
2 imaginary

## II. Discriminant

**If we had two  
real roots...**

(look at example #1)

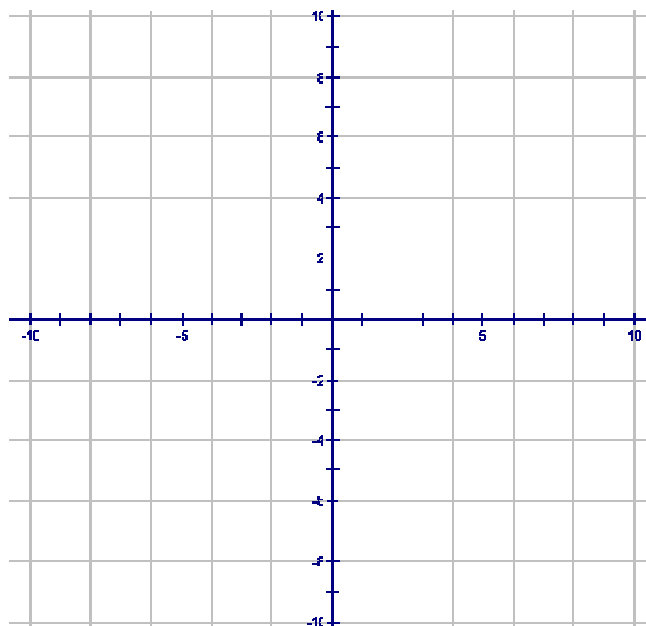




## II. Discriminant

**If we had one real  
root...**

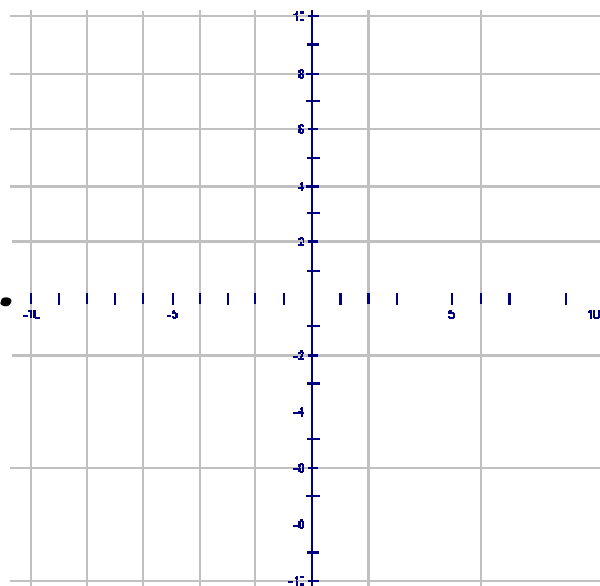
(look at Example #2)

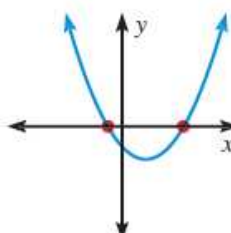
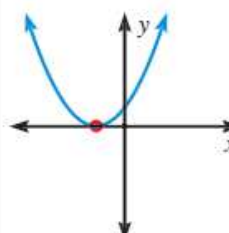
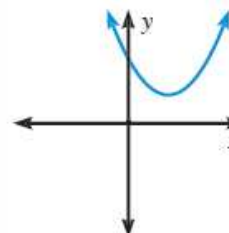


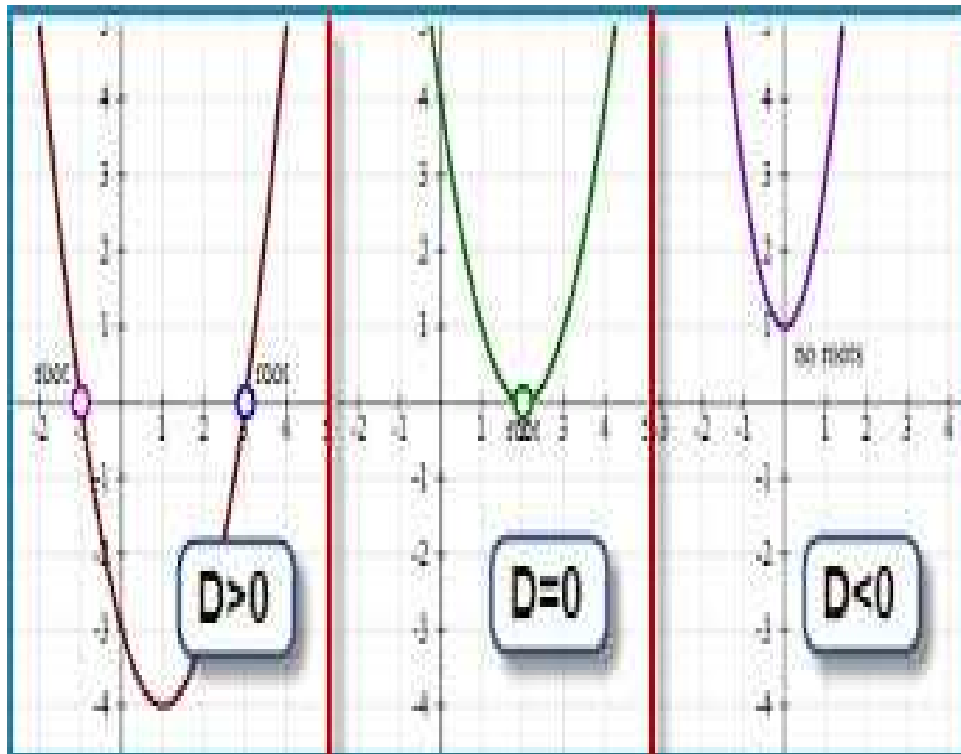
## II. Discriminant

**If we had two  
imaginary roots...**

(look at Example #3)



| KEY CONCEPT   |   | <i>For Your Notebook</i>  |   |  |
|---|---|---|---|--|
| <b>Using the Discriminant of <math>ax^2 + bx + c = 0</math></b> |   |   |   |  |
| <b>Value of discriminant</b>                                    | $b^2 - 4ac > 0$   | $b^2 - 4ac = 0$   | $b^2 - 4ac < 0$   |  |
| <b>Number and type of solutions</b>                             | Two real solutions  | One real solution   | Two imaginary solutions   |  |
| <b>Graph of <math>y = ax^2 + bx + c</math></b>                  |  <p style="text-align: center;">Two x-intercepts</p> |  <p style="text-align: center;">One x-intercept</p> |  <p style="text-align: center;">No x-intercept</p> |  |



### Warm Up

Find the discriminant of the quadratic equation and give the number and type of solutions of the equation.  $b^2 - 4ac$

1)  $8x^2 = 9x - 11$       $8x^2 - 9x + 11 = 0$       $(-9)^2 - 4(8)(11)$   
 $81 - 352$

2)  $2x^2 + 4x - 4 = 0$       $4^2 - 4(2)(-4)$   
 $16 + 32$

3)  $7x^2 - 2x = 5$

$7x^2 - 2x - 5$

$(-2)^2 - 4(7)(-5)$

$4 + 140$

$+$   
 2 real solution

$+$   
 2 real solutions

$-$   
 No real Roots

Let's take a break from the notes.....

## Solving WS (Best Method)

Step 1: Look at the problem and choose the "best" method for solving.

\*Let's discuss\*

Step 2: Solve the equation using the methods discussed in class.

$$\textcircled{10} \quad (x-2)(x+1) = 4$$
$$x^2 + 1x - 2x - 2 = 4$$

## III. Imaginary Numbers

As we enter the land of Oz....

$$\sqrt{-1} = i$$

$$i^2 = \sqrt{-1}^2$$

Let's use our imaginations..

$$i^2 = -1$$

$$i^3 = i^2 \cdot i^1 = -1i \text{ or } -i$$

$$i^4 = -1 \cdot i$$

$$i^4 = i^2 \cdot i^2$$

$$= -1 \cdot -1$$

$$= 1$$

| $i^0$ | $i^1$ | $i^2$ | $i^3$ | $i^4$ | $i^5$ | $i^6$ | $i^7$ | $i^8$ |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1     | $i$   | -1    | $-i$  | 1     | $i$   | -1    | $-i$  | 1     |

$$i^2 \cdot i^3$$

$$-1 \cdot -i$$

$$i^3 = i^2 \cdot i = -1 \cdot i = -i,$$

Examples:  $i^{27} = -i$

$$i^8 \cdot i^8 \cdot i^8 \cdot i^3$$

$$1 \cdot 1 \cdot 1 \cdot -i$$

II. Solve.

Examples

$$x^2 + 1 = 0$$



II. Solve.

Examples

$$x^2 + 6x + 18 = 0$$

$$ax^2 + bx + c$$

$$a=1 \quad b=6 \quad c=18$$

$$X = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$X = \frac{-6 \pm \sqrt{6^2 - 4(1)(18)}}{2(1)}$$

$$X = \frac{-6 \pm \sqrt{36 - 72}}{2}$$

$$X = \frac{-6 \pm \sqrt{-36}}{2} \left\langle \begin{array}{l} \sqrt{-1} \\ \sqrt{36} \end{array} \right.$$

$$X = \frac{-6 \pm 6i}{2}$$

$$X = \frac{-6 \pm 6i}{2}$$

$$X = -3 \pm 3i$$

II. Solve.

Examples

$$\frac{-3(x-4)^2}{-3} = \frac{18}{-3}$$

$$\sqrt{(x-4)^2} = \sqrt{-6}$$

$$x-4 = \pm \sqrt{-6} \quad \left\{ \begin{array}{l} \sqrt{-1} \\ \sqrt{6} \end{array} \right.$$

$$x-4 = \pm i\sqrt{6}$$

+4

$$x = 4 \pm i\sqrt{6}$$

II. Solve.

$$-6x^2 + 3x + 2 = 3$$

$$-6x^2 + 3x - 1 = 0$$

$$a = -6 \quad b = 3 \quad c = -1$$

$$x = \frac{-3 \pm \sqrt{9 - 4(-6)(-1)}}{2(-6)}$$

$$x = \frac{-3 \pm \sqrt{9 - 24}}{-12}$$

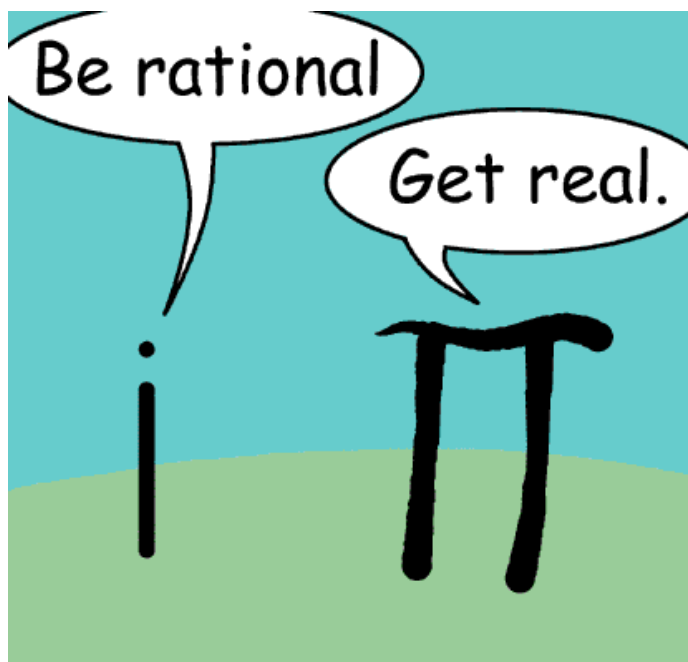
$$x = \frac{-3 \pm \sqrt{-15}}{-12} \quad \begin{matrix} \sqrt{-1} \\ \sqrt{15} \end{matrix}$$

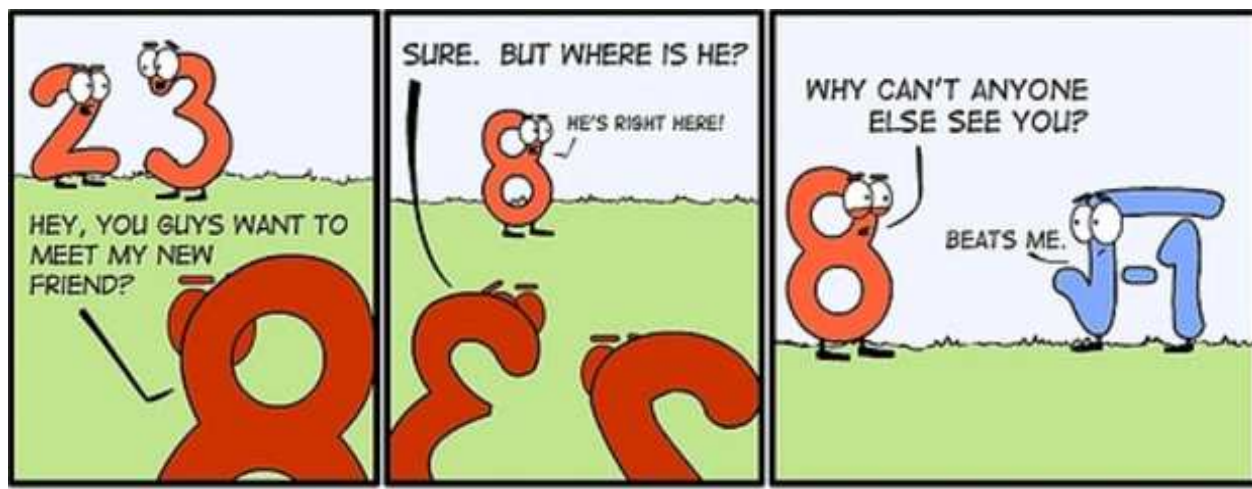
$$x = \frac{-3 \pm i\sqrt{15}}{-12}$$

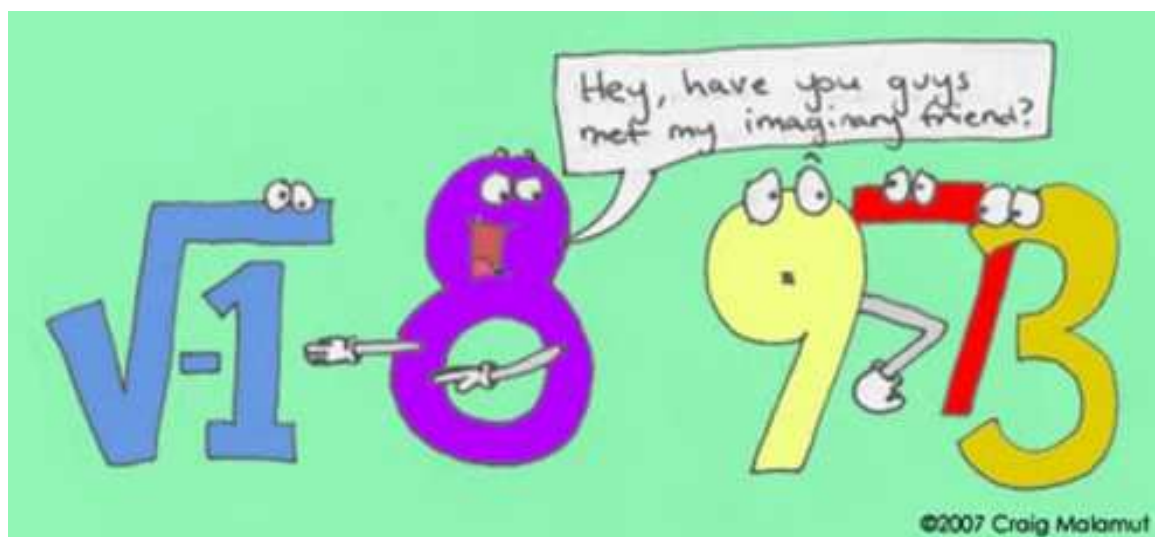
Examples

Placemat

Yellows ws







## III. Imaginary Numbers

$$\sqrt{-5} = \sqrt{-1 \cdot 5} = i\sqrt{5}$$

$$\sqrt{-\frac{1}{4}} = \sqrt{-1 \cdot \frac{1}{4}} = i\frac{1}{2} \text{ or } \frac{1}{2}i$$

$$\sqrt{-8} = \sqrt{-1 \cdot 4 \cdot 2}$$

$$i2\sqrt{2}$$

or

$$2i\sqrt{2}$$



### III. Imaginary Numbers

#### Real Numbers

$1, -3, 0, \pi, .5, -\frac{1}{98}$

#### Purely Imaginary Numbers

$i, -3i, i\sqrt{5}, \pi i$

#### Complex Numbers

$1+i, -3-2i, \pi+i$

$a+bi$  ← standard form

### III. Imaginary Numbers

To add and subtract  
complex numbers...

Add or subtract  
the real parts...

...and then add or  
subtract the imaginary  
parts!

$$1.) \quad (2 + 3i) + (5 - 2i) = 7 + i$$

## III. Imaginary Numbers

$$2.) (17 + 4i) - (18 - 5i) = -1 + 9i$$

$$3.) \overbrace{2(1+i)}^{2+2i} + (3+3i) = 5+5i$$

$2+2i + 3+3i$

$$4.) (-4) + \overbrace{2(3-i)}^{-4+6-2i} = 2-2i$$

## III. Imaginary Numbers

To multiply  
complex numbers...

**FOIL!!!!!!!!!!**

$$1.) (1+i)(2-3i) = 2 - 3i + 2i - 3i^2$$

$5 - i$

$$2.) (-3+i)(2-5i) = -6 + 15i + 2i - 5i^2$$

$-1 + 17i$

$$3.) (-4-i)(-4+i) =$$

$16 - 4i + 4i - i^2$

$-1(-1)$

$17$

Yellow ws

### III. Imaginary Numbers

Every complex number has a fraternal twin.

$$\underline{a + bi}$$

$$\underline{a - bi}$$

1.)  $4 + 3i$   $4 - 3i$

3.)  $1 - 6i$   $1 + 6i$

2.)  $\textcircled{-3} - 7i$   $-3 + 7i$

4.)  $-2i$   $2i$

### III. Imaginary Numbers

To divide complex numbers...

$$1.) \frac{(7+3i)(2+i)}{(2-i)(2+i)}$$

$$\frac{14 + 7i + 6i + 3i^2}{4 + 2i - 2i - i^2}$$

(-1)  
2

-1-1)

$$\frac{11 + 13i}{5}$$

## III. Imaginary Numbers

$$2.) \frac{4+7i}{-2-3i} \cdot \frac{-2+3i}{-2+3i} = \frac{(-8+12i-14i+21i^2)}{4-6i+6i-9i^2} = \frac{-29-2i}{13}$$

$$3.) \frac{1+2i}{4i} \cdot \frac{-4i}{-4i} = \frac{-4i-8i^2}{-16i^2} = \frac{8-4i}{16}$$



DLT

And the homework is....

Unit 2 Day 4/5

Solve using the Best Method ws-Quiz  
Friday and next Monday